

SPIRAL-LIKE FUNCTIONS ASSOCIATED WITH WRIGHT DISTRIBUTION SERIES

MALLIKARJUN G. SHRIGAN¹ AND SIBEL YALCIN²

ABSTRACT. The purpose of the present paper is to introduce a Wright distribution and obtain some sufficient conditions for analytic functions, whose coefficients are probabilities of the Wright distribution series, to belong to class of spiral-like univalent functions. Further, we discuss the geometric properties of an integral operator related to the Wright distribution series.

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¹ SCHOOL BASIC AND APPLIED SCIENCES, JSPM UNIVERSITY, PUNE, INDIA

² DEPARTMENT OF MATHEMATICS, FACULTY OF ARTS AND SCIENCES, UNIVERSITY OF BURSA ULUDAG, GÖRÜKLE, BURSA, TURKEY

Email address: ¹ mgshrigan@gmail.com, ² syalcin@uludag.edu.tr